

$$1) \tau_s = \frac{k(s+3)}{(s+4)(s^2+4s+5)}$$

$$ii) \sigma_a = [-4 - 2+j \quad -2-j] - (-3) = -5; \theta_a = \frac{72}{3-1} = 36^\circ$$

iii)

$$B) 10\% \text{ OS}, \zeta = 0.59, \omega_n = 4.08$$

i) closed loop poles dominant

$$\begin{aligned} \text{CL poles} &= -\zeta\omega_n + j\omega_n\sqrt{1-\zeta^2} \\ &= -2.41 + j 3.29 \end{aligned}$$

ii) k ;

sub cl into $\frac{1}{G(s)}$; $k=1$

$$\frac{(s+4)(s^2+4s+5)}{(s+3)}$$

$$k = 10.96$$

iii) validity

$$iv) \tau_s = \frac{4}{2.41}$$

$$= 0.83$$

$$\tau_p = \frac{\pi}{3.29}$$

$$= 0.95$$

ess =

Question 2

$$G(s) = \frac{K(s^2 - 2 + 8)}{(s+3)(s^2 + 4s + 5)}$$

dominant pole $j - 0.88 \pm j1.71$ & 20% overshoot

$$T_s = \frac{4}{|\text{real}|}$$
$$= \frac{4}{0.88}$$

$$= 4.55 \text{ s}$$

$$T_{s \text{ new}} = \frac{2}{5} 4.55 \quad \text{4 specification}$$
$$= 0.73$$

$$\xi = \frac{-\ln(0.2)}{\sqrt{\pi^2 + (\ln 0.2)^2}}$$
$$= 0.46$$

$$T_s \text{ new} = \frac{4}{\xi \omega_n}$$

$$\omega_n = \frac{4}{0.46 \times 0.73}$$

$$= 3.18$$

$$\text{Real CL poles} = -0.46 \times 3.18$$

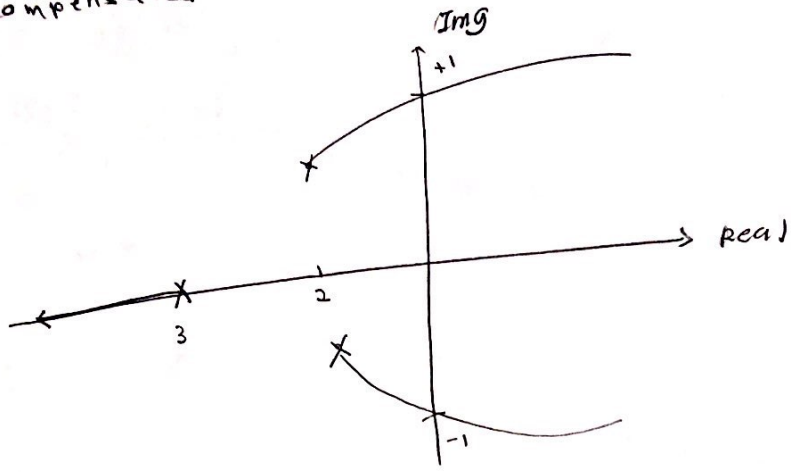
$$= -1.46$$

$$\text{Imag CL poles} = j 3.18 \sqrt{1 - 0.46^2}$$

$$= j 2.82$$

$$\text{CL poles} = -1.46 + j 2.82$$

uncompensated



$$G(s) = \frac{12}{s(s+6)}$$

$$|G(j\omega)| = \frac{21.58}{(-20 \log \omega) (\sqrt{\omega^2 + 6})}$$

ii) 20 rad/s

$$\frac{21.58}{(-20 \log 20) (\sqrt{20^2 + 6})}$$

$$= 0.04$$

