

Section 5

Q1)

a) i) Poles = $(s+4)$, $(s+2+j1)$, $(s+2-j1)$

Zero = $(s+3)$

$$G(s) = \frac{(s+3)}{(s+4)(s+2+j1)(s+2-j1)} = \frac{(s+3)}{(s+4)(s^2+4s+5)}$$

ii) $\sigma_a = \frac{(-4 -2+j1 -2 -j1) - (-3)}{3-1} = -2.5$

$\theta_a =$

$k=0$, $\theta_a = \frac{180^\circ}{2} = 90^\circ$

$k=1$, $\theta_a = \frac{180 \times 3}{2} = 270^\circ$

since there's only two asymptote

iii) $= \sum \theta_z - \sum \theta_p + 180$
 $= \tan^{-1}(\frac{1}{1}) - [\tan^{-1}(\frac{1}{2}) + 90] + 180$
 $= 108.43^\circ$

b) i) $\zeta = 0.59$ $\omega_n = 4.08 \text{ rad/s}$ $\sigma_s = 10\%$

i) $-\zeta \omega_n \pm j \omega_n \sqrt{1-\zeta^2} = -2.4 \pm j 3.29$

ii) $k = \frac{1}{|G(s)H(s)|} = \frac{(s+4)(s^2+4s+5)}{(s+3)} = 10.96$

iii) $1 + KGH = 0$

$$\frac{(s+3)}{(s+4)(s^2+4s+5)} + 1 = 0$$

$$\frac{(s+3)}{(s+4)(s^2+4s+5)} + \frac{(s+4)(s^2+4s+5)}{(s+4)(s^2+4s+5)} = 0$$

$$\frac{(s+3)(s+4)(s^2+4s+5)}{(s+4)(s^2+4s+5)} = 0$$

$$s^3 + 8s^2 + 21s + 20 + 10.96s + 32.88 = 0$$

$$s^3 + 8s^2 + 31.96s + 52.88 = 0$$

$$(s + 3.18)(s + 2.41 \pm j 3.29) = 0$$

$$s_1 = -3.18$$

$$s_2 = -2.4 + j 3.29$$

$$s_3 = -2.4 - j 3.29$$

~~3.14~~

$$\frac{3.18}{2.4} = 1.325 < 5$$

cannot use 2nd approximation method.

iv) T_s
 T_p
 e_{ss}

$$T_s = \frac{4}{2.4} = 1.67 \text{ s}$$

$$T_p = \frac{\pi}{3.29} = 0.95 \text{ s}$$

$$e_{ss} = \frac{1}{1+K_p}$$

$$K_p = \lim_{s \rightarrow 0} f(s) = 0.15$$

Q2)

$$G(s) = \frac{K(s^2 - 2s + 8)}{(s+3)(s^2 + 4s + 5)}$$

$$s_d = -0.88 \pm j1.72$$

$$\%OS = 20\%$$

$$\zeta = \frac{-\ln(20/100)}{\sqrt{\pi^2 + \ln^2(20/100)}} = 0.46$$

$$\zeta \omega_n = 0.88$$

$$(0.46) \omega_n = 0.88$$

$$\omega_n = 1.91 \text{ rad/s}$$

$$T_{s \text{ new}} = \frac{3}{5} T_{s \text{ old}}$$

$$T_{s \text{ old}} = \frac{4}{0.88} = 4.55$$

$$= \frac{3}{5} (4.55)$$

$$= 2.73$$

$$T_{s \text{ new}} = 2.73 = \frac{4}{\zeta \omega_n}$$

$$\omega_n = \frac{4}{2.73(0.46)} = 3.185$$

Real

Q3)

$$G(s) = \frac{12}{s(s+6)}$$

$$1 - G(s) = \frac{12}{6} \frac{1}{s(s/6 + 1)}$$

$$i) \quad |G(j\omega)| = \frac{12}{\omega \sqrt{\omega^2 + 6^2}}$$

$$|G(j\omega)| \text{ in dB} = 20 \log 12 - 20 \log \omega - 20 \log \sqrt{\omega^2 + 6^2}$$

$$ii) \quad 6.02 \text{ dB} - 38.78 \text{ dB}$$

$$= -32.74 \text{ dB}$$

$$h) \quad G(s) = \frac{100}{s+10} \quad 20 \log 10 = 20 \text{ dB}$$

$$= \frac{100}{100} \left(\frac{1}{s/10 + 1} \right)$$

